

## Parallel Performance Analysis for CUDA-Based Co-rank Framework on Bipartite Graphs Heterogeneous Network

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**Abstract**—The Co-rank is a ranking algorithm based on bipartite graphs of heterogeneous networks, which has been extensively studied and employed in the past decades. The Co-rank algorithm can utilize all kinds of objects in heterogeneous networks. However, the computational complexity of Co-rank algorithm limits its application on large scale datasets. Considering the efficiency of computation, we parallelize the algorithm with CUDA. We demonstrate our method via large-scale experiments across drug-target datasets and obtain excellent speedup. The results show that the optimization effect of Co-rank on the GPU platform is obvious.

**Keywords**—CUDA; parallel computing; Co-Rank Framework; Bipartite Network.

### I. INTRODUCTION

The social nature of the network makes it contain a large number of heterogeneous network resources. There are at least two or more types of vertices and edges in a heterogeneous network. Compared to the network which has only one type of node, heterogeneous networks can bring more information. Heterogeneous network models are widely used in Web services [1-3], social networks [4-5] and biological networks [6-7], which are used to predict unknown information.

The Co-rank is a ranking algorithm based on bipartite graphs of heterogeneous networks, which has been extensively studied and employed in the past decades. The Co-rank algorithm can utilize all kinds of objects in heterogeneous networks. For example, [8] used Co-rank algorithm predicting authors and their publications, and [9] propose a bi-type ranking algorithm to joint documents and authors in a bibliographic network, [10] is proposed to determine the importance of the objects and relationships of multiple relational data at the same time.

Due to the complexity of heterogeneous networks, the complexity of computation increases linearly with the number of network nodes, which brings more challenges to computation. In order to improve the efficiency of data processing, many parallel methods are proposed for heterogeneous networks. For example, [11-13] have proposed parallel computing model for PageRank and random walk. [14] provided an implementation of CUDA parallel to PageRank. [15] proposed parallel scheme of SimRank in Mapreduce.

Single core computing power is weaker than the CPU in the Many Integrated Cores, but the concurrency is much higher than the CPU. Some graphic processing chip

manufacturers have found that the hardware features of GPU make it very suitable for parallel computing with high concurrency [16-17]. Therefore, GPGPU provides an important means for parallel computing in the way of coprocessor. GPU has been used in many fields of scientific computing. Such as computational fluid dynamics [18-19], bioinformatics [20-21], etc. Co-rank can be regarded as an iterative matrix vector multiplication, and CUDA is especially good at such calculations.

In this research, we design a Co-rank network to describe drug-target and predict the missing edges between drug and target. As the number of nodes in the network increases, the computational complexity of the algorithm increases proportionally. Considering the efficiency of computation, we parallelize the algorithm. Therefore, we do some parallelization on the Co-rank drug-target algorithm of hybrid heterogeneous network based on CUDA.

### II. METHOD

#### A. Bipartite Heterogeneous Network Model of Drug-Target

A heterogeneous network contains two networks with different types of nodes and edges, as well as a bipartite graph containing bipartite associations between them [22]. Suppose the graph  $G_D = (V_D, E_D)$  with  $V_D = \{v_{d1}, v_{d2}, \dots, v_{dn}\}$ ,  $G_T = (V_T, E_T)$  with  $V_T = \{v_{t1}, v_{t2}, \dots, v_{tm}\}$ . And the bipartite graph connecting  $G_D$  and  $G_T$  is  $G_B = \{V_D \cup V_T, E_B\}$  with  $E_B = V_D \times V_T$ . The bipartite heterogeneous network can be defined of  $G_B = (V_B, E_B)$  as:  $V_B = \{V_D \cup V_T\}$ ,  $E_B = \{E_D \cup E_T \cup E_{DT}\}$

#### B. Construction of Heterogeneous Network

This heterogeneous network was composed of a drug-drug similarity network, a target network, and a bipartite graph containing drug-target associations. The walk on the above three networks, four state transition probability matrices ( $P_D, P_T, P_{DT(n \times m)}$  and  $P_{TD(m \times n)}$ ) need to establish for jump between the two networks.

We define  $A_{D(n \times n)}$ ,  $A_{T(m \times m)}$ ,  $A_B$  as their respective adjacency matrix, then the transition probabilities can be computed based on adjacency matrix.

### (1) Drug-drug similarity network: $P_D$

Let  $A_{D(n \times n)}$  be the adjacency matrix of a drug network with  $n$  number of nodes.  $P_{D(i,j)}$  represent the probability of transition from node  $i$  to node  $j$ . The calculation of  $P_{D(i,j)}$  is given as Equation (1).

$$P_{D(i,j)} = \begin{cases} A_{D(i,j)} / \sum_{k=1}^n A_{D(i,k)} & \text{if } e(i,j) \in E \\ 0, & \text{otherwise} \end{cases} \quad (1)$$

### (2) Target-target interactive network: $P_T$

$A_{T(m \times m)}$  is the adjacency matrix of a target network with  $m$  number of nodes, if there is a interaction between  $t_i$  and  $t_j$ , then  $A_{T(i,j)} = 1$ . The probability of transition matrix of target-target interactive network is given by Equation (2).

$$P_{T(i,j)} = \begin{cases} A_{T(i,j)} / \sum_{k=1}^m A_{T(i,k)} & \text{if } e(i,j) \in E \\ 0, & \text{otherwise} \end{cases} \quad (2)$$

### (3) Inter-network transfer matrix: $P_{DT}$ and $P_{TD}$

$A_B$  is the adjacency matrix of the drug-target bipartite network as Equation (3),  $P_{DT}$  is the transition matrix from the drug network to the target network.

$$A_{B(i,j)} = \begin{cases} 1 & \text{if } d_i \text{ is related with } t_j \\ 0, & \text{otherwise} \end{cases} \quad (3)$$

So the probability of transition matrix  $P_{DT}$  which can be given by the Equation (4).

$$P_{DT(i,j)} = \begin{cases} A_{B(i,j)} / \sum_j A_{B(j,i)} & \text{if } \sum_j A_{B(j,i)} \neq 0 \\ 0, & \text{otherwise} \end{cases} \quad (4)$$

Similarly,  $P_{TD}$  can be given by the Equation (5).

$$P_{TD(i,j)} = \begin{cases} A_{B(i,j)} / \sum_j A_{B(i,j)} & \text{if } \sum_j A_{B(i,j)} \neq 0 \\ 0, & \text{otherwise} \end{cases} \quad (5)$$

### C. Co-rank on the drug-target network

Co-rank framework [10] based on the bipartite graph and random walk with restart algorithm. We take drug-target network as an example to describe the Co-rank framework. The Co-rank consists of two types of random walk, one is a random walk of the intra-network. A random walk in drug similarity network  $G_D$  and target interaction network  $G_T$ . For example, there is a link between node  $d_i$  and  $d_j$ , which are exactly from  $G_D$ . The random walker can move from  $d_i$  to its link neighbor  $d_j$  node with probability  $\alpha$  ( $\alpha \in (0, 1)$ ) or move back to its home node with the restart probability  $1-\alpha$ . The other is a random walk between networks based on the bipartite graph  $G_B$  network. If a random walker on the  $G_D$  and moves to a bridging node, it can jump to the other network  $G_T$  with a probability  $\lambda$  ( $\lambda \in (0, 1)$ ) and takes  $2k+1$  inter-network steps or move back to the other nodes in its home subnet with the probability  $1-\lambda$  take  $m$  intra-network steps walk on  $G_D$ . A transition probability matrix is denoted as  $P$  in the following Equation (6).

$$P = \begin{bmatrix} (\alpha)P_T^m & (1-\alpha)P_{TD}(P_{DT}P_{TD})^k \\ (1-\alpha)P_{DT}(P_{TD}P_{DT})^k & (\alpha)P_D^n \end{bmatrix} \quad (6)$$

Computational complexity of algorithm is  $\mathbf{O}(t * (2k + 1) * n_D * n_T) + \mathbf{O}(n * n_T^3 + m * n_D^3)$ . The computational time complexity of the algorithm is high, so we consider using CUDA to parallelize it.

## III. CUDA PARALLEL OF CO-RANK

### A. Parallel Scheme

The flow diagram of parallel Co-rank algorithm based on CUDA is shown in Fig.1. The calculation procedure is divided into two parts. The host needs to calculate the transition matrix  $P_D, P_T, P_{DT}, P_{TD}$  according to the adjacency matrix  $A_D, A_T, A_B$ . Cudamallochost is used to allocate the unified memory for host and device of the transition matrix. The device calculate matrix power for  $P_D$  and  $P_T$ , and then calculate matrix multiplication for  $P_{TD}$  and  $P_{DT}$ , so as to obtain the probability matrix  $P$ . Then calculate  $y^t$  iteratively, and finally copy  $y$  from the device back to the host.

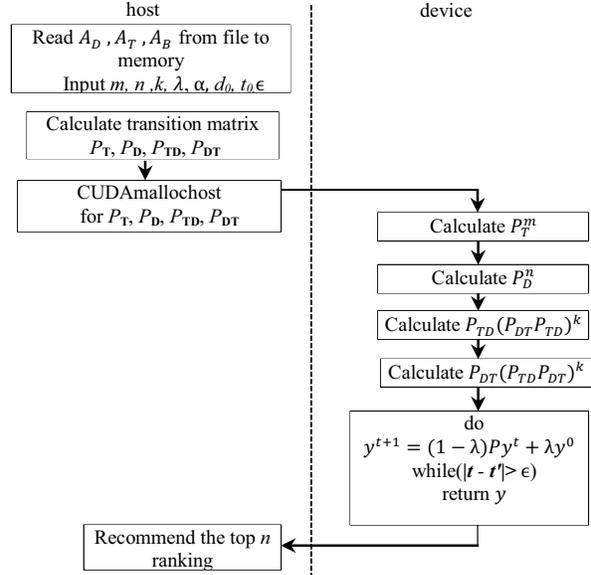


Figure 1. CUDA Parallel Scheme of Co-rank

### B. Parallelization of Co-rank based on CUDA

The NVIDIA's CUDA CUBLAS library [23] provides matrix multiplication function. In addition, Cusparsv function in CUSPARSE library [24] realizes the sparse matrix and vector multiplication function. The specific algorithm process is as follows.

#### Algorithm process: Parallelization of Co-rank based on CUDA

**Procedure**  $Cu\_Co\_rank(P_D, P_T, P_{DT}, P_{TD}, m, n, k, \lambda, \alpha, d_0, t_0)$

- 1: Allocate the variable memory space on GPU device and copy  $P_D, P_T, P_{DT}, P_{TD}, m, n, k, \lambda, \alpha, d_0, t_0$  from CPU to GPU;
  - 2: Initialization solution vector  $d_0, t_0$  on GPU;
  - 3: Call Cusparsv\_powermatrixmul( $*P_T, m$ );
  - 4: Call Cusparsv\_powermatrixmul( $*P_D, n$ );
  - 5: Call CuBiWalk( $*P_{DT}, *P_{TD}, k$ );
  - 6: Call CuBiWalk( $*P_{TD}, *P_{DT}, k$ );
  - 7: **Repeat**
  - 8: Call  $cusparsv\_csrsv$  function compute  $(1-\lambda)P y^t + \lambda y^0$
  - 9: **while**( $|y - y'| > \epsilon$ )
  - 10: return  $y$
  - 11: copy  $d, t$  from GPU to CPU;
- End Procedure**

#### IV. RESULTS AND DISCUSSION

In this paper, we used drug and target dataset to test our approach. And we compared our algorithm with RWR (Random Walk Restart) to evaluate accuracy and calculation performance.

##### A. Experiment environment

The computing platform of this paper is as following: CPU is Intel(R) Core(TM) i7-4790, 3.6GHz, 16GB host memory; GPU is GeForce GTX 850M with 4GB device memory. We use NVIDIA CUDA toolkit v9.0 libraries and GCC 5.4.0 compilation.

##### B. Dataset

Drug dataset and drug-target bipartite graph dataset were obtained from Drug Bank, DGIDB and TTD databases, which were described in document [25]. Drug dataset gives the structure similarity between the 606 drugs. Drug-target bipartite graph dataset contains drug and its corresponding target. We used PPI (Protein-Protein Interaction) as target-target interaction dataset, PPI dataset was obtained from the Human Protein Reference Database (<http://www.hprd.org/>) which included 39240 interactive information between 9673 proteins. So  $n$  of adjacency matrix  $A_{D(n \times n)}$  is 606,  $m$  of adjacency matrix  $A_{T(m \times m)}$  is 9673.

##### C. Evaluating accuracy

In this paper, we use the Leave-one-out cross validation to evaluate the accuracy of our algorithm.

In order to evaluate the effectiveness of the algorithm in drug target prediction as accurately as possible. We selected drugs which include targets greater than or equal to 2 in the bipartite network as test data. The dataset includes 450 drugs with 2960 corresponding drug-target relationships. In the test, we set the network parameters as follows:  $m=5$ ,  $n=6$ ,  $k=1$ ,  $\lambda=0.5$ ,  $\alpha=0.6$ . And adopted the following test method[26]. For example, for drug  $d$ , its drug targets include target  $t$ .

(1) First, removing the corresponding relationship between  $d$  and  $t$  in the binary graph network  $G_D$  and  $D_G$ . Then initialing vector  $d_0$  with the remaining known targets of  $d$ , running the Cu\_Co-rank algorithm to predict. Finally, we obtained the ranking results of all the predicted targets corresponding to drug  $d$ .

(2) For each drug  $d$ , recording the prediction ranking of its removed target  $t$ .

(3) After 2960 groups of tests, the ROC and Recall curves were obtained through statistical calculation of all the test results.

By observing the ROC diagram shown in Fig.2, we find that with the increase of threshold, the prediction accuracy of Cu\_Co-rank algorithm has been greatly improved compared with the RWR algorithm. From Fig.3 of the RECALL curve, we find that the results of the Cu\_Co-rank algorithm is better than RWR algorithm. When the  $n$  is near to 800, the algorithm obtain more than 0.9 accuracy, and the RWR algorithm is only 0.65. The result show that the Cu\_Co-rank algorithm was more effective in predicting.

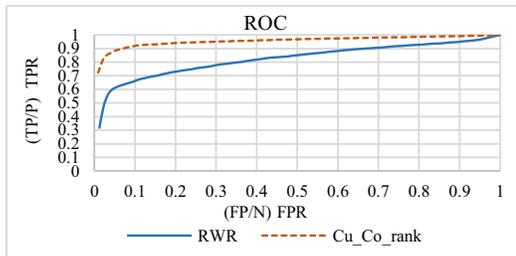


Figure 2. ROC Curve of Cu\_Co\_rank and RWR

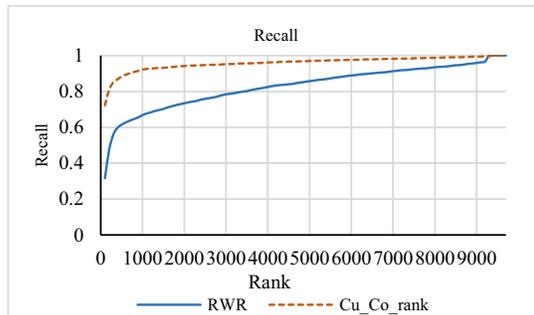


Figure 3. Recall Curve of Cu\_Co\_rank and RWR

##### D. Performance and Speedup

###### (1) Target interaction network calculation

Target interaction network has 9,673 nodes and 3,9240 relationships. This network structure diagram is a typical sparse matrix, so we use sparse matrix to calculate. When the test data set is 5000, the CPU computation time of the test data set is nearly 30 minutes, so the comparison between GPU and CPU acceleration ratio only calculates the data within 5000, and the results are as follows Table 1 and Fig.4.

TABLE 1. GPU/CPU SPEEDUP AND SPARSE\_GPU/CPU SPEEDUP

Dataset	GPU/CPU Speedup	Sparse_GPU/CPU Speedup
50	0.00313699	0.001478835
100	0.026307628	0.009525391
500	2.643575467	2.937666715
1000	28.24542319	40.70232975
1500	68.32913795	78.91968159
5000	210.0562152	347.9921199

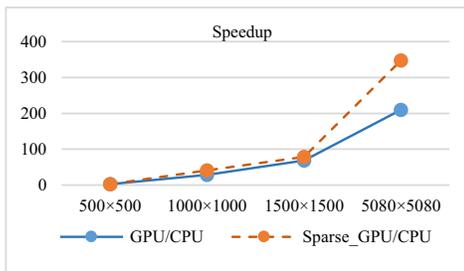


Figure 4. Speedup of GPU/CPU and Sparse\_GPU/CPU

## (2) The computation results of matrix multiple power

Since the transfer matrix  $P$  needs to calculate the multiple power multiplication of  $P_D$  matrix and  $P_T$  matrix. We test it with GPU and CPU, and the results are shown in below Fig.5.

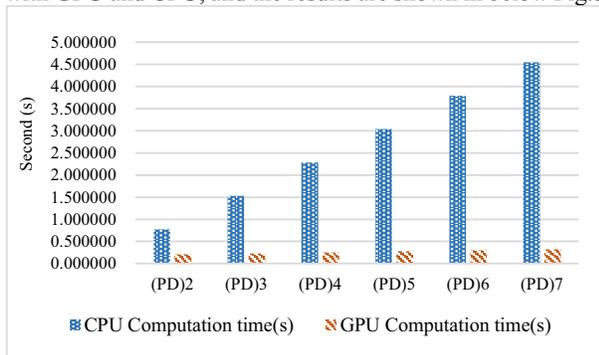


Figure 5. Calculation time of multiple power multiplication for  $P_D$  with GPU and CPU

## V. CONCLUSIONS AND FUTURE WORK

In this paper, we propose a GPU accelerated Co-rank algorithm based on bipartite graph heterogeneous network. First, we apply the Co-rank algorithm framework to the drug target heterogeneous network, and verify the effectiveness of the algorithm. The ROC and Recall curves of the algorithm are all superior to the RWR algorithm. Secondly, for the computational complexity of Co-rank algorithm on large data sets, we propose a parallel computing model based on CUDA. The test results show that the algorithm has a significant acceleration effect. This makes it possible to apply Co-rank algorithm to large scale datasets in desktop computer.

In future work, we hope to test the algorithm's parameters and performance on larger data sets. In addition, in order to further improve the computational efficiency, we need to optimize the Cu\_Co-rank algorithm by data partitioning, sparse storage and texture memory.

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